Bioengineering 280A Principles of Biomedical Imaging

Fall Quarter 2005 MRI Lecture 3

TI I DESCRIPTION E IL SON

MR signal is Fourier Transform

$$\begin{split} s(t) &= \int_{x} \int_{y} m(x, y) \exp\left(-j2\pi \left(k_{x}(t)x + k_{y}(t)y\right)\right) dx dy \\ &= M\left(k_{x}(t), k_{y}(t)\right) \\ &= F\left[m(x, y)\right]_{k_{x}(t), k_{y}(t)} \end{split}$$





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K-space

At each point in time, the received signal is the Fourier transform of the object

$$s(t) = M(k_x(t), k_y(t)) = F[m(x, y)]_{k_x(t), k_y(t)}$$

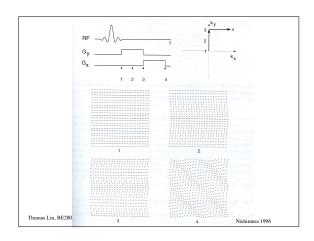
evaluated at the spatial frequencies:

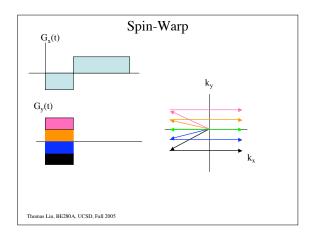
$$k_x(t) = \frac{\gamma}{2\pi} \int_0^t G_x(\tau) d\tau$$

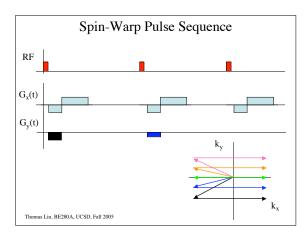
$$k_{y}(t) = \frac{\gamma}{2\pi} \int_{0}^{t} G_{y}(\tau) d\tau$$

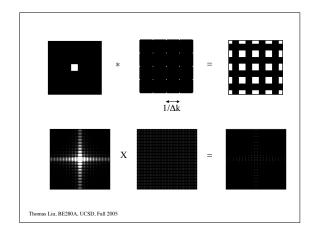
Thus, the gradients control our position in k-space. The design of an MRI pulse sequence requires us to efficiently cover enough of k-space to form our image.

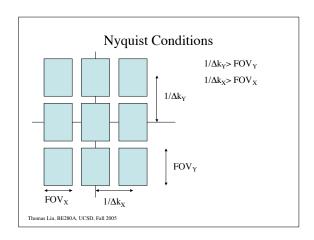
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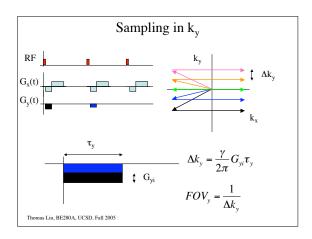


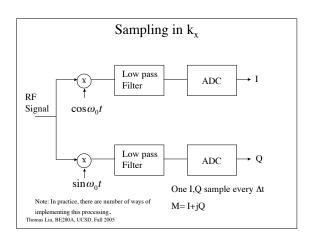


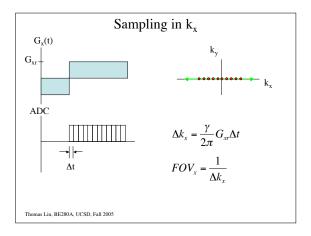


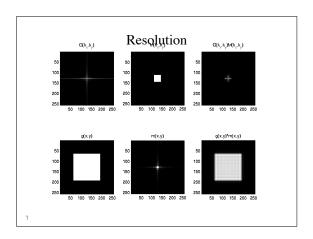










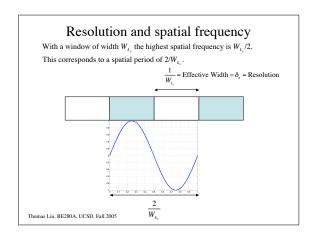


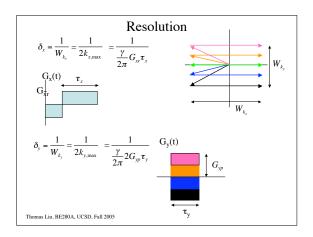
Effective Width
$$w_E = \frac{1}{w(0)} \int_{-\infty}^{\infty} w(x) dx$$
Example
$$w_E = \frac{1}{1} \int_{-\infty}^{\infty} \operatorname{sinc}(W_{k,x}) dx$$

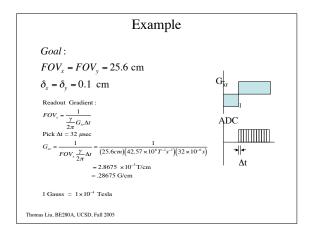
$$= F[\operatorname{sinc}(W_{k,x})]_{k_k=0}$$

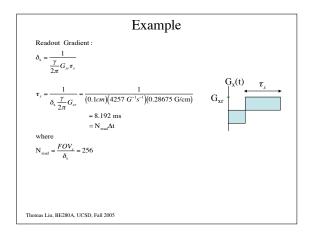
$$= \frac{1}{W_{k_k}} \operatorname{rect}\left(\frac{k_x}{W_{k_k}}\right)_{k_k=0}$$

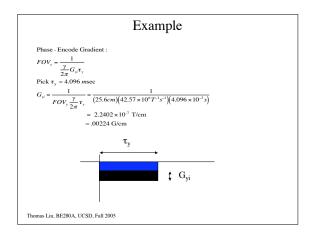
$$= \frac{1}{W_{k_k}}$$
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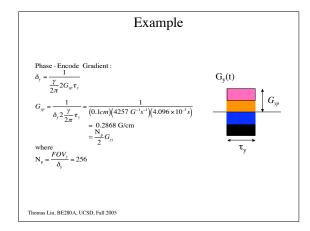


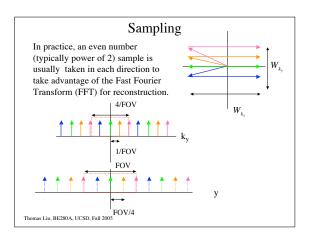


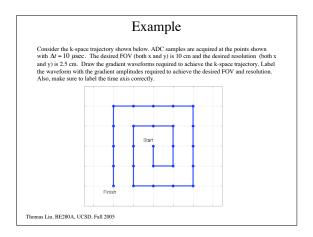


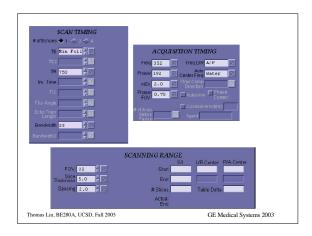


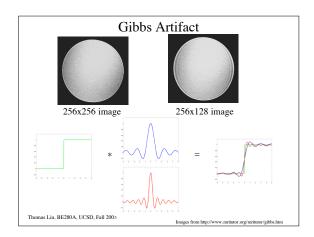


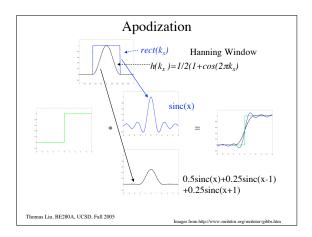


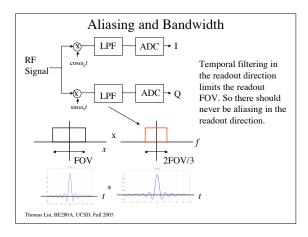


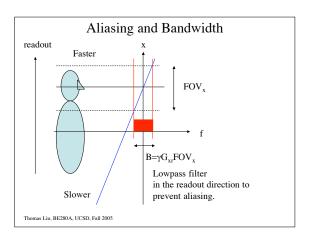


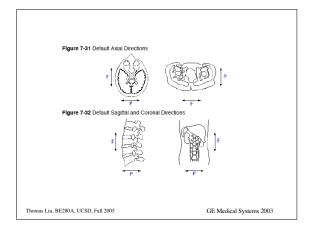












Slice Selection

Recall, that we can tip spins away from their equilibrium state by applying a radio-frequency pulse at the Larmor frequency.

In the presence of a spatial gradient G_z , spins in an interval $-\Delta z/2$ to $-\Delta z/2$ have Larmor frequencies ranging from ω_0 - $\gamma G_z \Delta z/2$ to ω_0 + $\gamma G_z \Delta z/2$. In order to tip all the spins in this interval, we can apply an RF pulse with energy that is spaced over this frequency interval.

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